

# Final Presentation

Development of  $\text{BaTiO}_3$  Ceramic High Dielectric Pellets for a Capacitor using a Solid State Synthesis method involving Hand Milling, Calcining, Pressing and Sintering

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# Introduction (Overview)

- ❖  $\text{BaTiO}_3$  is a widely used dielectric in capacitors due to its high dielectric constant and permittivity.
- ❖ Perovskite crystal structure ( $\text{ABX}_3$ ),  $\text{Ba}^{2+}$  and  $\text{Ti}^{4+}$  ions shift under an applied electric field that creates a permanent dipole moment that allows charge to be stored.  
(Spontaneous below Curie temp)
- ❖ For solid state synthesis of  $\text{BaTiO}_3$  (hand milling, calcination, sintering) the following reaction is used (1:1)

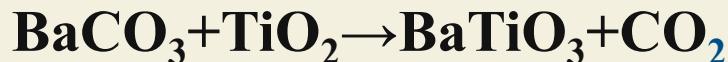
$$\text{BaTiO}_3 = 233.192 \text{ g/mol}$$

$$\text{BaCO}_3 = 197.336 \text{ g/mol}$$

$$\text{TiO}_2 = 79.866 \text{ g/mol}$$

$$10 \text{ g } \text{BaTiO}_3 \times \frac{1 \text{ mol } \text{BaTiO}_3}{233.192 \text{ g}} \times \frac{1 \text{ mol } \text{BaCO}_3}{1 \text{ mol } \text{BaTiO}_3} \times \frac{197.336 \text{ g}}{1 \text{ mol } \text{BaCO}_3} = 8.462 \text{ g } \text{BaCO}_3$$

$$10 \text{ g } \text{BaTiO}_3 \times \frac{1 \text{ mol } \text{BaTiO}_3}{233.192 \text{ g}} \times \frac{1 \text{ mol } \text{TiO}_2}{1 \text{ mol } \text{BaTiO}_3} \times \frac{79.866 \text{ g}}{1 \text{ mol } \text{TiO}_2} = 3.425 \text{ g } \text{TiO}_2$$



# Abstract

Using an equimolar ratio of  $\text{BaCO}_3$  and  $\text{TiO}_2$  that was hand milled to achieve to a particle size of less than 750 nm, calcined for 4 hours at 950°C to form  $\text{BaTiO}_3$  and pressed into pellets and sintered at 1350°C for 3 hours, we found a dielectric constant of 300 at room temperature (25°C), a density of 4.58 g/cm<sup>3</sup> (76% theoretical of 6.02 g/cm<sup>3</sup>) and a grain size of about 6  $\mu\text{m}$ . We also found single phase purity of the pellets. Since we expected a dielectric of 1000, a density of 5.1 g/cm<sup>3</sup> and a grain size of less than 1  $\mu\text{m}$  we determined the root cause of not meeting these expected values to be non uniform particle size which created inhomogenous regions and non equimolar combination of precursors that led to porosity that lowered the dielectric constant.

# Design of Experiment

- ❖ We are testing particle size, phase purity, density, grain size, and density. The first 2 of these are observations rather than factors for our experiment. Three remaining factors to examine are density, grain size, and density.
- ❖ Based on a  $2^3$  factorial experiment (MiniTab), there are 8 samples needed for this experiment total with a confidence level of 95% ( $\alpha = 0.05$ )
  - 3 factors: dielectric constant, grain size, density
  - 2 levels: with sintering and without sintering
- ❖ By conducting experiments in the order of SEM (grain size), density, and then dielectric constant we were able to reduce the number of replicates needed from 16 to 8.

| WORKSHEET 2           |          |                     |      |                         |                     |         |               |
|-----------------------|----------|---------------------|------|-------------------------|---------------------|---------|---------------|
| Full Factorial Design |          |                     |      |                         |                     |         |               |
| Design Summary        |          |                     |      |                         |                     |         |               |
| Factors:              | 3        | Base Design:        | 3, 8 | Resolution with blocks: | IV                  |         |               |
| Runs:                 | 8        | Replicates:         | 1    |                         |                     |         |               |
| Blocks:               | 2        | Center pts (total): | 0    |                         |                     |         |               |
| Block Generators: ABC |          |                     |      |                         |                     |         |               |
| Alias Structure       |          |                     |      |                         |                     |         |               |
| I                     |          |                     |      |                         |                     |         |               |
| Blk = ABC             |          |                     |      |                         |                     |         |               |
|                       |          |                     |      |                         |                     |         |               |
| C1                    |          | C2                  |      | C3                      |                     | C4      |               |
| StdOrder              | RunOrder | CenterPt            |      | Blocks                  | Dielectric Constant | Density | Particle Size |
| 1                     | 8        | 1                   | 1    | 2                       |                     | 1       | 1             |
| 2                     | 5        | 2                   | 1    | 2                       |                     | 1       | -1            |
| 3                     | 7        | 3                   | 1    | 2                       |                     | -1      | -1            |
| 4                     | 6        | 4                   | 1    | 2                       |                     | -1      | 1             |
| 5                     | 1        | 5                   | 1    | 1                       |                     | -1      | -1            |
| 6                     | 4        | 6                   | 1    | 1                       |                     | -1      | 1             |
| 7                     | 3        | 7                   | 1    | 1                       |                     | 1       | -1            |
| 8                     | 2        | 8                   | 1    | 1                       |                     | 1       | 1             |
| 9                     |          |                     |      |                         |                     |         |               |
| 10                    |          |                     |      |                         |                     |         |               |

Figure 1:

# Design of Experiment

## Hypotheses for Goal Values:

1. **Dielectric Constant** – One-Sided t test
  - a. Null:  $\mu_{\text{exp}} < 1000$
  - b. Alternative:  $\mu_{\text{exp}} \geq 1000$
  
1. **Density** – Two-Sided t test for 85% theoretical of  $6.02 \text{ g/cm}^3$ 
  - a. Null:  $\mu_{\text{exp}} = 5.1 \text{ g/cm}^3$
  - b. Alternative:  $\mu_{\text{exp}} \neq 5.1 \text{ g/cm}^3$
  
1. **Particle Size** – One-Sided t test
  - a. Null:  $\mu_{\text{exp}} \geq 1\mu\text{m}$
  - b. Alternative:  $\mu_{\text{exp}} < 1\mu\text{m}$

# Workflow- Procedure

Weigh out a 1:1 ratio of  $\text{BaCO}_3$  and  $\text{TiO}_2$ , grind up separately (1 hour)

- 10g total; 4 1g experimental pellets, 4 1g control-pellets

(10g from 8.462 g  $\text{BaCO}_3$  + 3.425g  $\text{TiO}_2$ )

SEM to check precursor particle sizes approximately equivalent before combining

Mix precursors and grind further, SEM for  $\text{BaTiO}_3$  particle size

Calcine at 950°C in furnace for 4 hours.  
(put sample in before ramping at 2°C/min then hold)

If grain size not small enough

If not right phase purity

Measure dielectric constant (LCR Meter), Density (Archimedes), Particle Size (SEM)

Sinter at 1350 °C 3 hours (literature suggests sintering between 1300°–1400 °C)

Press (at 150 MPa) into 8 1g  $\text{BaTiO}_3$  pellets

XRD to ensure phase purity ( $2\theta = 20^\circ - 80^\circ$ )  
→ grind again if multi-phase particles

# Deviations from original proposal

- ❖ XRD for phase purity: not as phase pure as desired, but unable to calcine again due to time restraints
  - With enough time, would have re-calcined
  - Likely will result in lower density and dielectric constant than initially expected
- ❖ Furnace time ended up being larger than expected due to ramp up and down times, this increased the overall cost of the furnace by a small amount. (Sintering 350°C for 3 hours)

# Particle Size of Individual Precursors

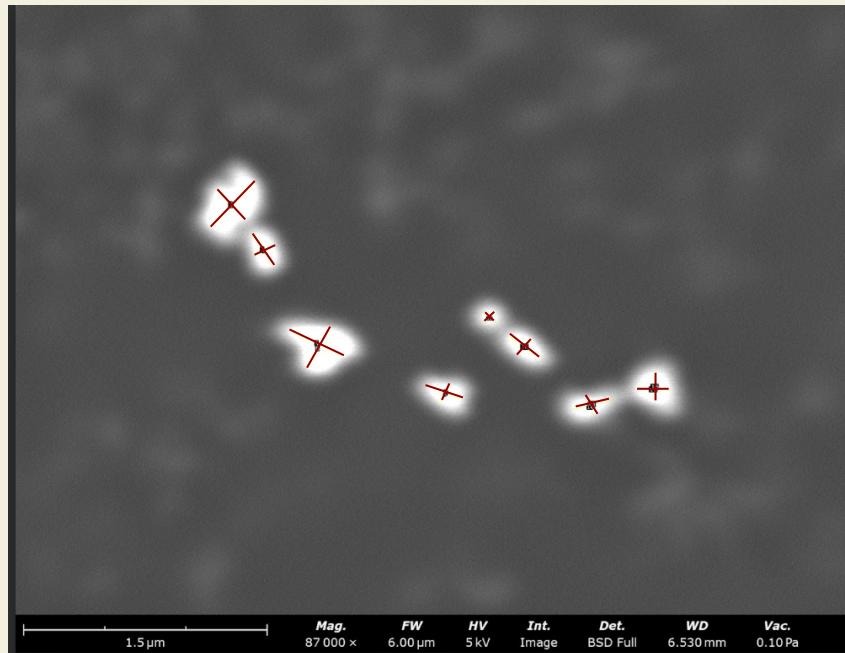


Figure 2: SEM of  $\text{BaCO}_3$

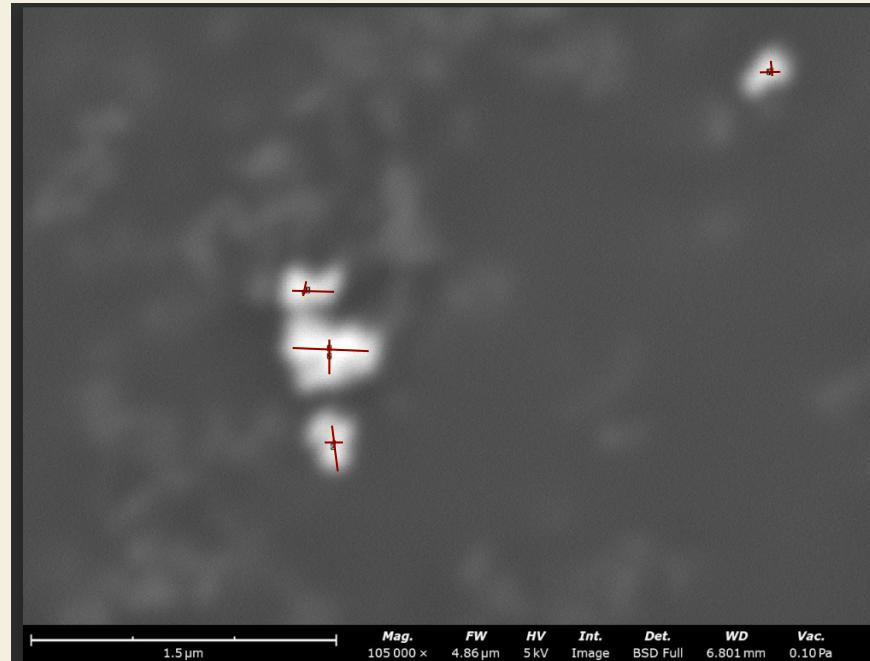


Figure 3: SEM of  $\text{TiO}_2$

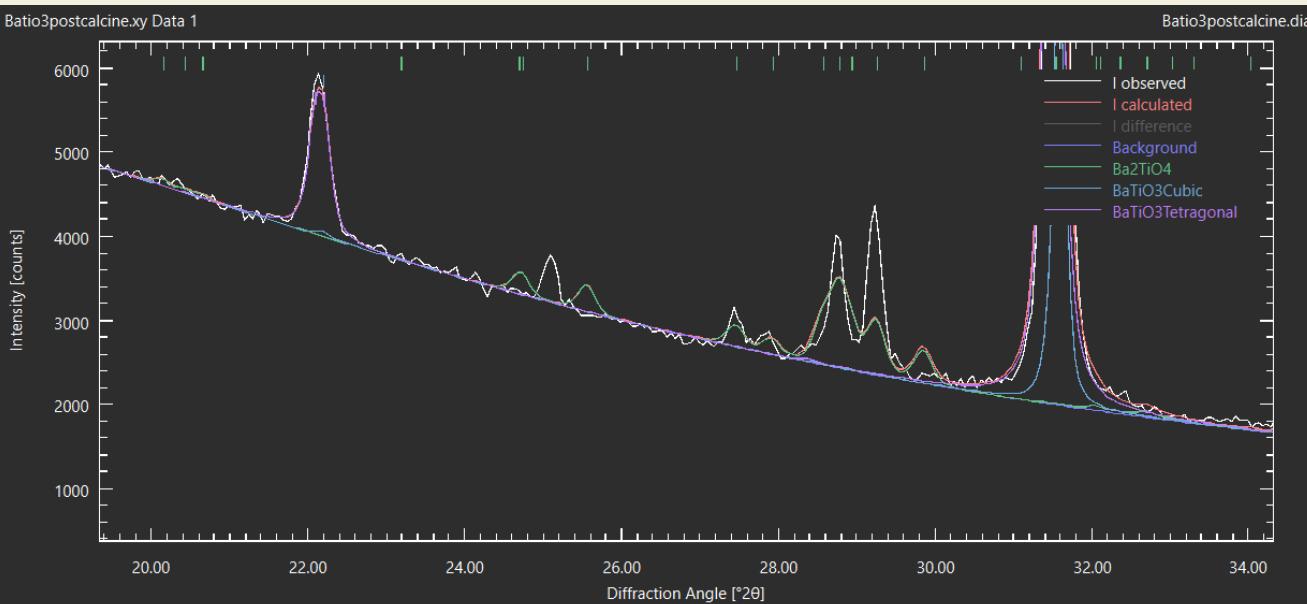
# Particle Size of Individual Precursors - Methods

- 3 images were taken of each sample of  $\text{BaCO}_3$  and  $\text{TiO}_2$  and all of the particles on the image were measured (at least 5 per image)
- Each measurement consisted of an x and y distance/diameter of the particle through ImageJ
  - The x and y diameters were averaged for each particle and are shown below
  - The standard error was calculated for the total x and y data sets from:  $\text{SE} = \sigma/\sqrt{n}$ 
    - Sigma is the standard deviation and n is the sample size

| Material        | Direction | Average            | Standard Deviation | Variance |
|-----------------|-----------|--------------------|--------------------|----------|
| $\text{TiO}_2$  | x         | $153.511 \pm 18.5$ | 97.71              | 9547.68  |
| $\text{TiO}_2$  | y         | $139.216 \pm 9.3$  | 49.15              | 2415.76  |
| $\text{BaCO}_3$ | x         | $234.381 \pm 22.8$ | 116.29             | 13524.25 |
| $\text{BaCO}_3$ | y         | $144.667 \pm 21.3$ | 104.79             | 10981.73 |

# XRD Spectra of Powder - Post Calcining

After Calcining, XRD Spectra of powder matched up most peaks with expected  $\text{BaTiO}_3$  with some  $\text{Ba}_2\text{TiO}_4$  peaks as a byproduct formed during calcination.  $\text{Ba}_2\text{TiO}_4$  has a dielectric constant of 40 when synthesized via solid state methods and this may have affected our final values for dielectric constant.<sup>1</sup>



$\text{BaTiO}_3$  Cubic: 17.3%

$\text{BaTiO}_3$  Tetragonal: 64.5%

$\text{Ba}_2\text{TiO}_4$ : 18.2%

Figure 4: Profex image of XRD after calcination process

# XRD Spectra - Post Calcining

- 64.5% tetragonal in red spectra

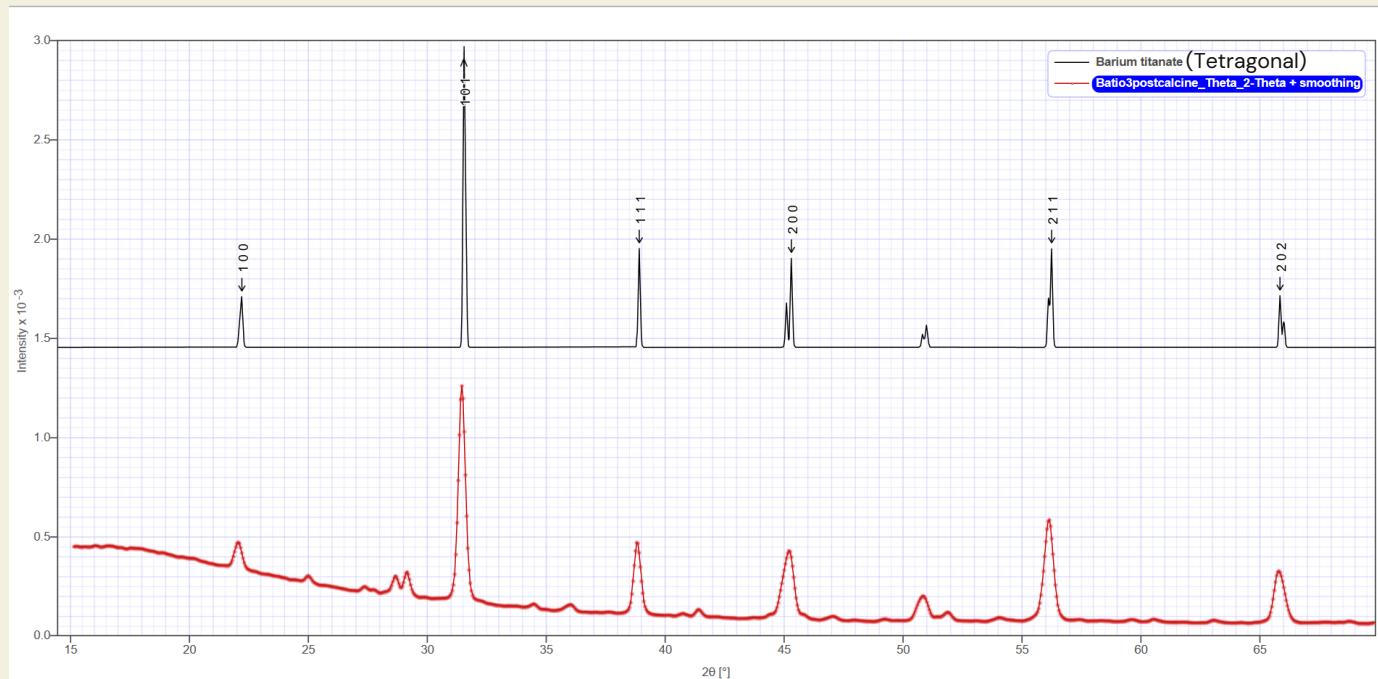


Figure 5: XRD of sample overlaid with CIF file after calcining

# XRD - Post Sintering

- ❖ Post-sinter XRD results are inconclusive due to researcher error.
- ❖ The black spectra is not representative of the post-sintered pellet

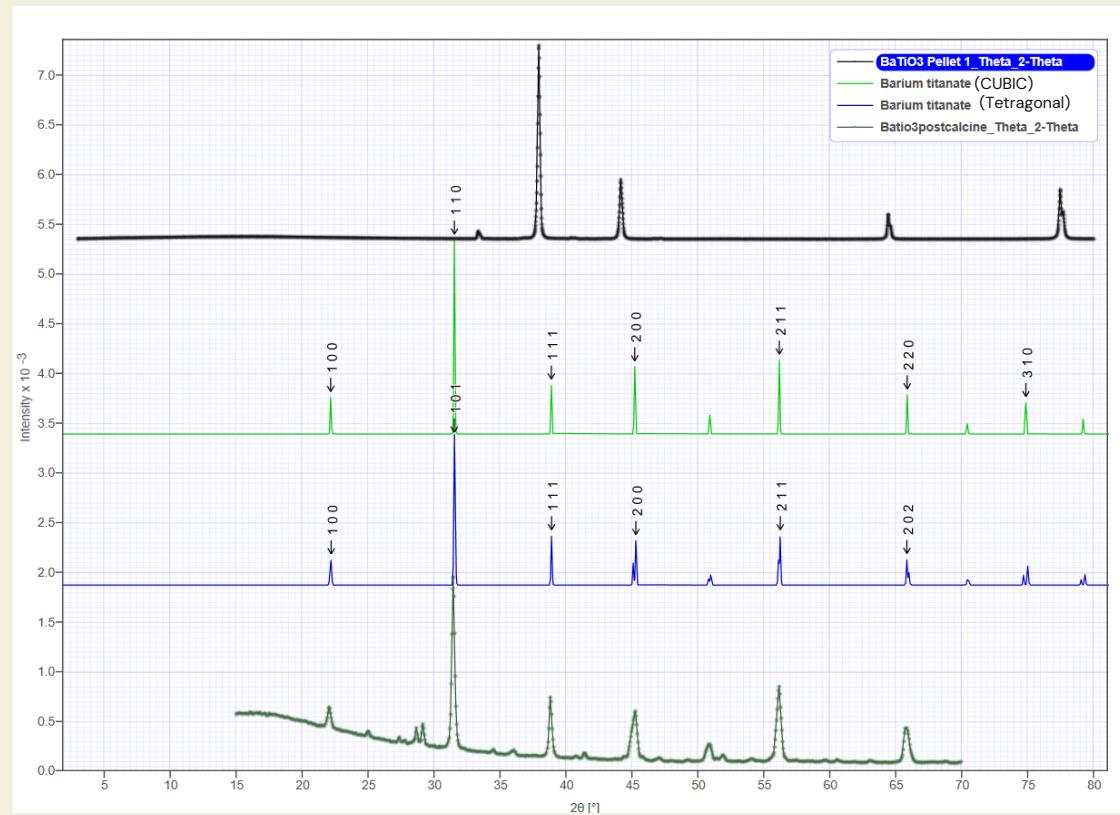


Figure 6: XRD overlay comparing our samples (pre & post sintered) to crystallography cif files

# Density and Porosity of Pellets

| Pellet             | Archimedes Density (g/cm <sup>3</sup> ) | Theoretical Density (g/cm <sup>3</sup> ) | Porosity (%)        |
|--------------------|---|--|---------------------|
| 1                  | Sheared                                 | Sheared                                  | Sheared             |
| 2                  | 1.925 ± 0.46                            | 4.739 ± 0.22                             | 59.368 ± 7.74       |
| 3                  | 4.949 ± 0.46                            | 4.638 ± 0.22                             | 6.712 ± 7.74        |
| 4                  | 5.657 ± 0.46                            | 4.657 ± 0.22                             | 21.475 ± 7.74       |
| 5                  | 5.036 ± 0.46                            | 4.577 ± 0.22                             | 10.027 ± 7.74       |
| 6                  | 4.656 ± 0.46                            | 3.361 ± 0.22                             | 38.542 ± 7.74       |
| 7                  | 5.080 ± 0.46                            | 5.065 ± 0.22                             | 0.289 ± 7.74        |
| 8                  | 4.808 ± 0.46                            | 3.883 ± 0.22                             | 23.817 ± 7.74       |
| <b>Average</b>     | <b>4.587 ± 0.46</b>                     | <b>4.417 ± 0.22</b>                      | <b>3.854 ± 7.74</b> |
| Standard Deviation | 1.22                                    | 0.59                                     | 20.48               |
| Variance           | 1.48                                    | 0.34                                     | 419.42              |

Table 2: Density and porosity values for each pellet

**Archimedes:**

$$\rho = (m_{\text{air}}) / (m_{\text{air}} - m_{\text{ethanol}}) * \rho_{\text{ethanol}}$$

**Bulk:**

Vol. of pellet is  $\pi(R^2)(t)$

R is radius, t is thickness of pellet

$$\text{So } \rho_{\text{bulk}} = (m_{\text{air}}) / \pi(R^2)(t)$$

**Porosity:**

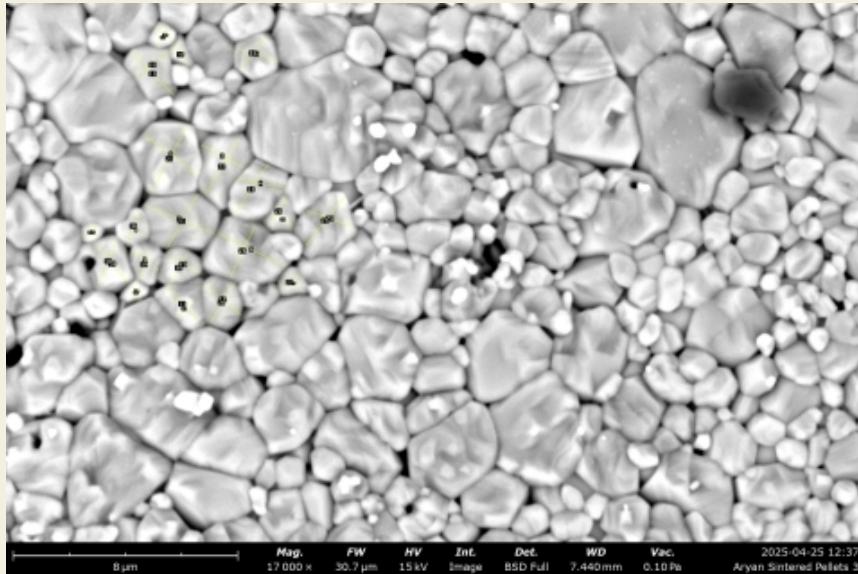
$$1 - (\rho_{\text{bulk}} / \rho)$$

**Percent Theoretical:**

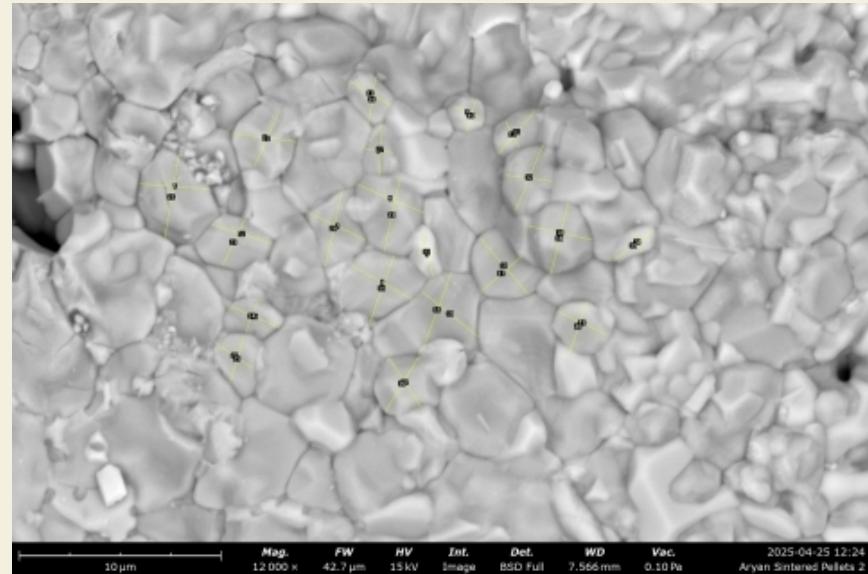
$$(4.587/6.02)*100\% = 76.2\%$$

Theoretical Density

# Grain Size (SEM)



Figures 8: Annotated images of the polished pellet surface under the SEM



Figures 9: Annotated images of the polished pellet surface under the SEM

# Grain Size (SEM)

- 4 pellets were imaged under SEM. 3 images were taken per sample, and within each image at least 15 measurements were made
- Each measurement consisted of an x and y distance/diameter of the grain through ImageJ
  - The x and y diameters were averaged for each pellet and are shown below
  - The standard error was calculated for the total x and y data sets from:  $SE = \sigma/\sqrt{n}$ 
    - Sigma is the standard deviation and n is the sample size

| Sample  | Average X ( $\mu\text{m}$ ) | Average Y ( $\mu\text{m}$ ) |
|---------|-----------------------------|-----------------------------|
| 1       | 6.877                       | 6.7809                      |
| 2       | 4.28062963                  | 4.289074074                 |
| 3       | 4.314695652                 | 4.667326087                 |
| 4       | 3.815103448                 | 3.38637931                  |
| Average | 4.821857183                 | 4.780919868                 |

Table 3: Average grain size of pellets

# Dielectric Constant (LCR Agilent 4284A LCR Meter)

| Pellet         | Dielectric                          | Standard Deviation | Variance |
|----------------|-------------------------------------|--------------------|----------|
| 2 - Front      | $339.1 \pm 1.49$                    |                    | 3.64     |
| 2 - Front      | $338.61 \pm 1.49$                   |                    |          |
| 2 - Front      | $335.32 \pm 1.49$                   |                    |          |
| 2              | $331.79 \pm 1.49$                   |                    |          |
| 2              | $330.81 \pm 1.49$                   |                    |          |
| 2              | $331.91 \pm 1.49$                   |                    |          |
| 4 - Front      | $222.45 \pm 1.80$                   |                    | 4.41     |
| 4 - front      | $214.25 \pm 1.80$                   |                    |          |
| 4 - front      | $213.49 \pm 1.80$                   |                    |          |
| 4              | $212.23 \pm 1.80$                   |                    |          |
| 4              | $211.34 \pm 1.80$                   |                    |          |
| 4              | $210.08 \pm 1.80$                   |                    |          |
| 5 - front      | $345.26 \pm 0.66$                   |                    | 1.63     |
| 5 - front      | $345.26 \pm 0.66$                   |                    |          |
| 5 - front      | $345.66 \pm 0.66$                   |                    |          |
| 5              | $345.26 \pm 0.66$                   |                    |          |
| 5              | $342.43 \pm 0.66$                   |                    |          |
| 5              | $342.03 \pm 0.66$                   |                    |          |
| <b>Average</b> | <b><math>297.63 \pm 14.4</math></b> |                    |          |

Table 4: Dielectric values for 3 pellets

- ❖ Out of the 7 pellets that did not shear, 3 of them were deemed best for LCR testing due to them being the most planar and clean (polished).
- ❖ Dielectric Constant (K) was calculated using the formula below:

$$K = C * t / (\epsilon_0 * A)$$

- C is Capacitance
- t is thickness of pellet
- A is Area of Contact (Pellet)
- $\epsilon_0$  is vacuum permittivity

# Data Analysis - Dielectric Constant

- ❖ One-sided t-test conducted with a focus on the right tail in MATLAB
- ❖ Null hypothesis failed to be rejected
  - With a 5% confidence interval, we did not achieve the goal dielectric constant
- ❖ Percent error calculation: 70.237% error

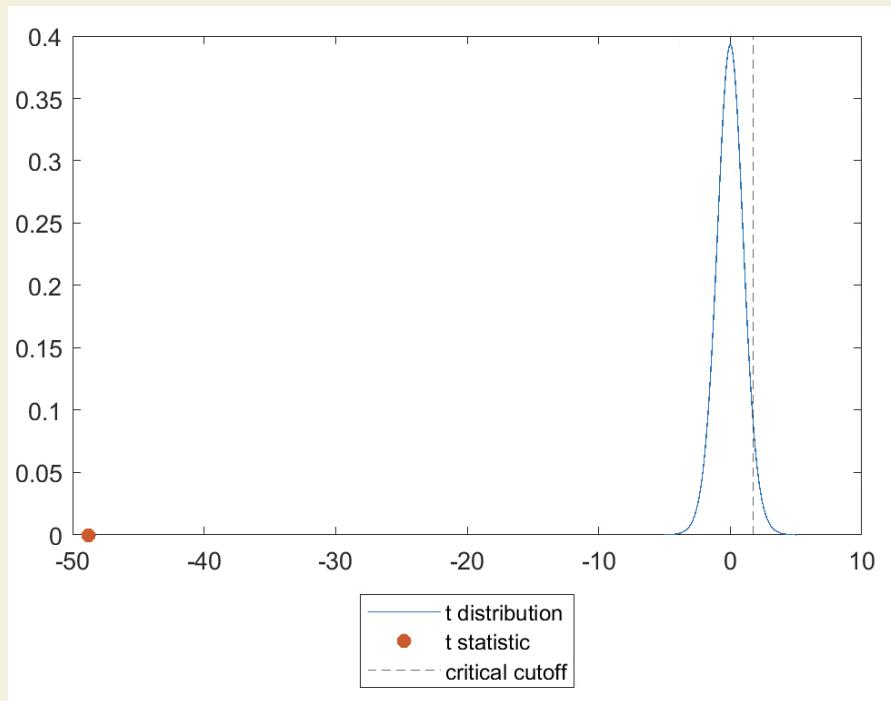


Figure 10: T-test graph for the dielectric constant

# Data Analysis - Density

- ❖ Two-sided t-test conducted in MATLAB
- ❖ Null hypothesis failed to be rejected
  - With a 5% confidence interval, we did not achieve the goal density
- ❖ However, percent error reveals:
  - 10.05% error from the goal mean
  - 76.2% of total theoretical density

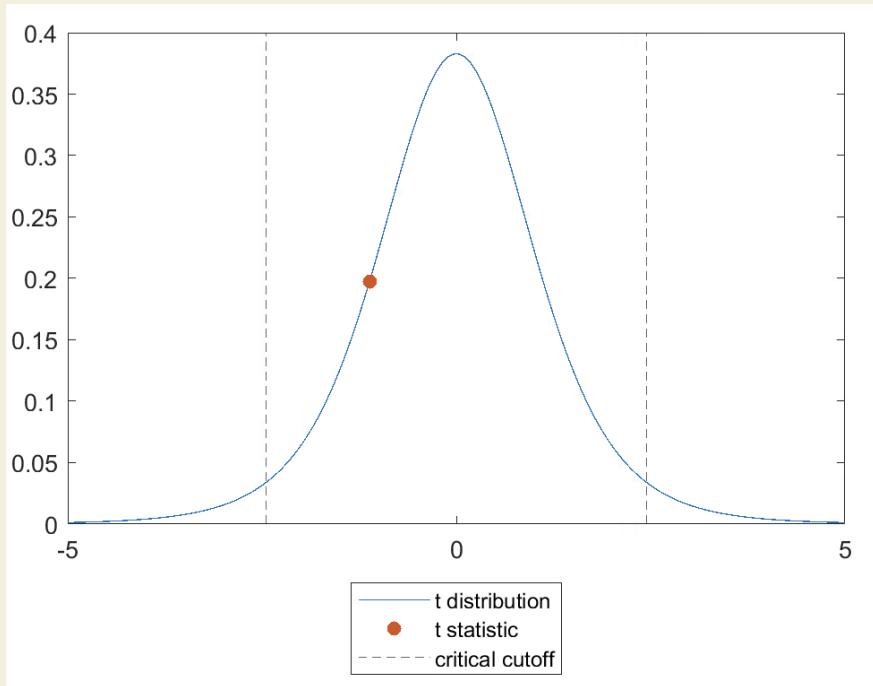


Figure 11: T-test graph for the density of pellets

# Data Analysis - Grain Size

- ❖ One-sided t-test conducted with a focus on the left tail in MATLAB
- ❖ Null hypothesis failed to be rejected
  - With a 5% confidence interval, we did not achieve the goal grain size

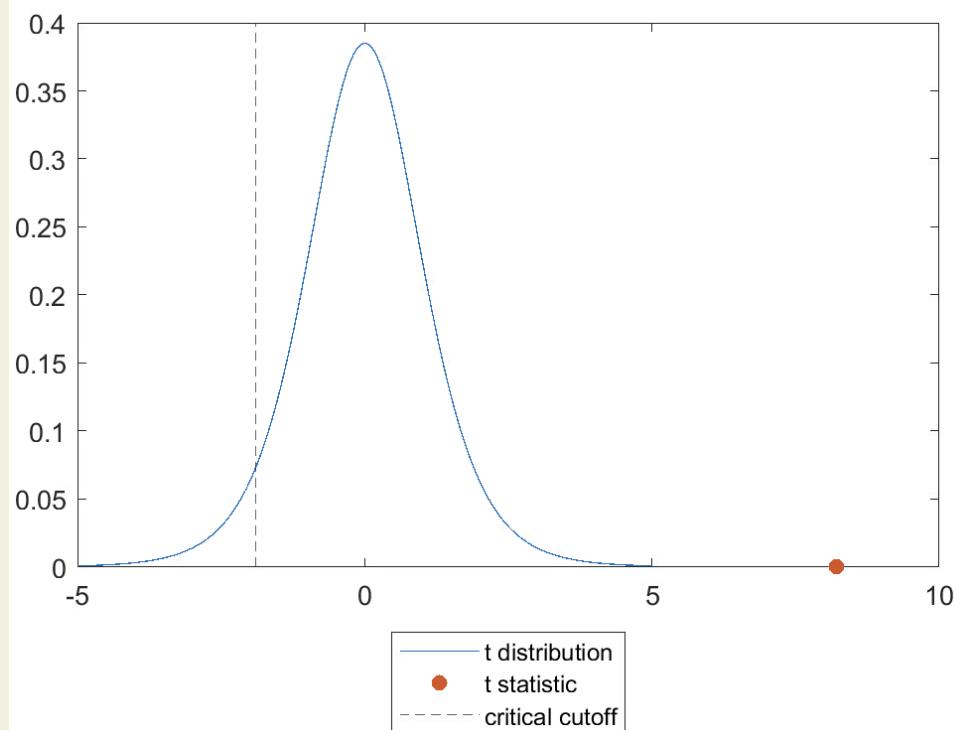


Figure 12: T-test graph for the grain size of pellets

# Final Parameters

|                     | Value                  | Pass or Fail  |
|---------------------|------------------------|---|
| Density             | 4.58 g/cm <sup>3</sup> | <b>Fail</b><br>(76% of expected)<br><b>Expected: 5.1 g/cm<sup>3</sup></b> |
| Dielectric Constant | 300                    | <b>Fail</b><br>(30% of expected)<br><b>Expected: 1000</b>                 |
| Grain Size          | 6.34 µm x 7.00 µm      | <b>Fail</b><br>(600% of expected)<br><b>Expected: 1µm</b>                 |

# Root Cause Analysis:

- Inconsistent particle size with a variation of  $\pm 10\%$  for BaCO<sub>3</sub> and  $\pm 5\%$  for TiO<sub>2</sub> led to imperfect phase growth.
  - **BaTiO<sub>3</sub>** Cubic: 17.3%, **BaTiO<sub>3</sub>** Tetragonal: 64.5%, **Ba<sub>2</sub>TiO<sub>4</sub>**: 18.2%
- The imperfect phase distribution led to uneven grain sizing post sintering
  - Uneven grains lead to increased porosity
- Due to reduced phase purity and uneven grain growth from uneven precursor particle, the dielectric constant was drastically reduced to 300.

# Amended Budget (Final Costs)

| Material/Equipment                  | Amount/Usage | Cost (\$) |
|-------------------------------------|--------------|-----------|
| BaCO <sub>3</sub>                   | 8.462 (g)    | 0.42      |
| TiO <sub>2</sub>                    | 3.425 (g)    | 0.31      |
| Weighing Scale                      | -            | -         |
| Mortar and Pestle                   | 1 (week)     | 100       |
| Furnace                             | 46.5 (hours) | 1162.5    |
| Hydraulic Press                     | 2 (hours)    | 50        |
| SEM                                 | 2 (hours)    | 80        |
| XRD                                 | 2 (hours)    | 140       |
| Agilent 4284A LCR Meter             | -            | -         |
| Density Determination Kit (ethanol) | -            | -         |
| Miscellaneous                       | -            | 0         |

|                         | Expected   | Actual     |
|-------------------------|------------|------------|
| <b>Total Cost</b>       | \$1,550.73 | \$1,533.23 |
| <b>Price per Pellet</b> | \$193.84   | \$219.03   |

- ❖ Total cost was lower than expected by \$17.50
- ❖ Since 1 pellet sheared, only 7 successful pellets made
  - Cost per pellet higher than expected by \$25.19

Table 5: Amended budget values

# Future Recommendations

- ❖ Improve techniques used
  - Improve hand milling technique: Standardize grinding time, pressure, and motions during hand milling to achieve **finer and more uniform particle sizes**.
  - Handle powders and pellets carefully: Minimize contamination and mechanical damage during transfers, especially before sintering.
  - Enhance pressing techniques: Apply more consistent pressure and polish pellet surfaces better to improve dielectric measurements.
- ❖ Perform additional tests
  - Additional XRD, possibly TGA, DSC, or other tests to help determine phase purity
- ❖ Reassess heat-treatment parameters: ie. experiment with slightly lower sintering temperatures (1300–1325°C) or shorter times to prevent abnormal grain growth.
  - Recalcine to achieve highest possible phase purity of tetragonal phase
- ❖ Another possibility for a future experiment could be the addition of dopants to increase dielectric constant
  - Lanthanum or Strontium

# References

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8. Cost list for materials and analysis techniques 2016-1.pdf